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## Static vs. Dynamic Policies for Vehicle Routing Problems with Backhauling and Dynamically Arising Customer Demands

by

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#### Abstract

Dynamic<sup>\*</sup>

# Static vs. Dynamic Policies for Vehicle Routing Problems with Backhauling and Dynamically Arising Customer Demands

#### Abstract

Dynamic vehicle routing problems (VRP) have attracted more attention than dynamic vehicle routing problems with backhauling (VRPB) in the relevant literature. Dynamic VRPB are more complex than dynamic VRP, and since VRP are a special case of VRPB, models and algorithms for dynamic VRPB can easily be adapted for dynamic VRP. In this paper, we compare static vs. dynamic policies for solving dynamic VRPB with dynamically arising customer delivery and pickup demands. We develop MILP formulations and search algorithms for small-to-medium-sized problems under static and dynamic policies. Although dynamic policies are always at least as good as static policies, we observe from numerical experimentations that static policies perform relatively well for small-sized problems and low degrees of dynamism (*dod*). On the other hand, dynamic policies are expected to perform significantly better than static policies for large-sized problems, high degrees of dynamism (*dod*) and early availabilities of dynamic customer delivery and pickup demand information. We conclude the paper by providing directions for future research on dynamic VRPB.

**Keywords:** Vehicle routing problem; Backhauling; Split deliveries and pickups; Dynamic demand; Degree of dynamism; Static vs. dynamic policy

#### **1** Introduction

In the vehicle routing problem (VRP), a depot has to serve the linehaul demands of a set of customers with a fleet of vehicles. The objective is to determine the vehicle routes in order to minimize the total travelling time/cost of the vehicles. The problem is known to be NP-Hard. A number of variants of the basic VRP exist such as multiple depots, multiple time periods, time windows, service times, maximum route time limitations on vehicles and so on. An even more difficult problem is the vehicle routing problem with backhauling (VRPB) where a customer has

both linehaul and backhaul demands. It is intuitive that the VRP is a special case of the VRPB where the backhaul demands of customers are zero. Since both problems are NP-Hard, the solution approach in the literature so far has been the development of exact or mixed integer linear programming (MILP) formulations for solving small-sized problems and approximate or heuristic algorithms for solving medium to large-sized problems. For the different variants of the VRP/VRPB and their solution methodologies, readers are referred to *Laporte et al.* [8], *Ropke and Pisinger* [18] and *Mitra* [14].

The basic VRP/VRPB is static in the sense that all the information on customers, their demands, distances between locations, travelling times/costs and so on are known to the decision maker in the beginning of the planning period so that the solution to the problem, i.e. the vehicle routes remain static until the end of the planning period. However, in practice, much of the information may not be available at the time of decision-making, which may be revealed dynamically over time such as customer demands, travelling times and so on. This set of problems is referred to as the dynamic VRP/VRPB, which has produced a significant amount of research since about the last one-and-a-half decades. The dynamic VRP may consist of customers with delivery-only or pickup-only demands, dynamic customer requests and/or dynamic travel/service times, real-time diversions of vehicles en route to a customer or replanning of vehicle routes only when vehicles reach their next destinations, capacitated or uncapacitated vehicles, single time period or multiple time periods, single objective or multiple objectives, and so on. The solution approach for the different variants of the dynamic VRP has been re-optimization, i.e. the updation of vehicle routes as and when new information becomes available. Larsen et al. [9] defined an index called the degree of dynamism (dod) depending on the number of dynamic customer requests in comparison to the total number of customer requests for a setting with delivery-only customers, unknown service times, single objective function and updation of vehicle routes only at customer locations, and compared the performances of several routing policies with respect to the *dod*. Angelelli et al. [1, 2] compared the performances of static vs. dynamic policies and collaborative vs. individual dynamic transportation policies for a dynamic VRP with pickup-only and postponable or unpostponable customer requests, uncapacitated vehicles, multiple time periods and multiple objective functions allowing real-time diversions of vehicles en route to a customer. Wen et al. [19] developed an MILP formulation and a three-phase heuristic for a multi-period

dynamic VRP with delivery-only customer requests, capacitated vehicles, service time and maximum route time restrictions, and multiple objectives. The problem was solved on a rolling plan basis, and no real-time diversions of vehicles or updation of vehicle routes were allowed. Sensitivity analyses were carried out for the different parameters of the problem under consideration. *Lorini et al.* [11] extended an earlier model (*Potvin et al.* [15]) for a dynamic VRP with pickup-only customer requests, dynamic demands and travel times, uncapacitated vehicles, real-time diversions of vehicles and multiple objectives. They showed that real-time diversions of vehicles produced better results than the situation when updation of vehicle routes can only take place at customer locations (*Potvin et al.* [15]). For a detailed understanding of the different issues of the dynamic VRP and more comprehensive reviews of the related literature, readers may refer to *Psaraftis* [16, 17], *Gendreau and Potvin* [5], *Ichoua et al.* [7], *Ghiani et al.* [6] and *Larsen et al.* [10].

In contrast to the dynamic VRP, the dynamic VRPB has attracted less attention. The only related literature found was on dynamic pickup and delivery problems where vehicles pick up shipments from a set of customers to be delivered to another set of customers, which is clearly different from the setup of the dynamic VRPB. Interested readers may refer to

making no distinction between delivery and pickup vehicles. The same vehicle can cater to both delivery and pickup demands, and the route of the vehicle is managed dynamically as and when new customer requests arise. Since the dynamic characteristic of the problem may give rise to numerous possibilities, we had to narrow down the boundary of the problem. For example, since the vehicles are capacitated and the delivery and pickup requests from all the customers are not available at the beginning of the period, it is not known in advance how many vehicles would be needed to satisfy customer demands. Similarly, it is also not known in advance at how many points in time during the period new customer requests might arise dynamically. In this paper, we assume that a single vehicle would have sufficed had all customer delivery and pickup demands, known or unknown, been available at the beginning of the period, and there is only one another point in time during the period, other than the beginning of the period, when new customer demands might arise dynamically so that at most two vehicles would be needed to satisfy the delivery and pickup demands of all the customers. The purpose of these two assumptions is only to limit the boundary of the problem and facilitate numerical experimentations. It may be noted that the models and algorithms developed in this paper are applicable in practice to handle more dynamic situations. The major objective of this paper is to compare static vs. dynamic policies for such a problem setup. In the static policy, the route of a vehicle, once planned, is not changed thereafter, whereas in the dynamic policy, the route of a vehicle may change dynamically as and when new customer requests arise (It should be clear from the definitions of the policies that the models and algorithms for the static policy can easily be extended even if we relax the assumptions on the number of vehicles and the number of points in time when demands arise dynamically. To do the same for the dynamic policy, we need to keep track of the locations of the vehicles in real time, i.e. we need additional information on vehicle speeds/travelling times between locations and so on, which will lead us to make further assumptions. However, in practice, since all information is revealed dynamically over time, the models and algorithms may be suitably adapted and repeatedly run without any prejudice). The advantage of the static policy is reduced planning effort whereas the advantage of the dynamic policy is reduced travelling distance. Lund et al. [12] observed that static policies still performed relatively well for low degrees of dynamism (dod). Angelelli et al.

the customers on its route, demand information from customers that was not visible earlier becomes available and requires to be served. At this point, the decision maker has two choices – she may follow a static policy, i.e. she may not disturb the route of the first vehicle as originally planned and she may decide the route of the second vehicle to serve the customers whose demands originated later, or she may follow a dynamic policy that may alter the route of the first vehicle as originally planned, and simultaneously decides the routes of both the vehicles to serve the remaining customers planned to be served by the first vehicle and the new customers whose demands originated later. As per the descriptions of the policies, it is apparent that while in the static policy the routes of the vehicles are non-overlapping, in the dynamic policy there may be overlaps of the vehicle routes.

Both vehicles leave the depot with delivery loads (finished goods) only once and upon serving the customers on their respective routes return to the depot with pickup loads (returns). Split

			(1.1)
			(1.2)
0	0		(1.3)
0	0		(1.4)
		0	(1.5)
0	1		(1.6)

moment, the first vehicle is situated at customer location J, yet to be served, with delivery and pickup loads of FG and RT, respectively. The delivery and pickup demands of the customers already served by the first vehicle are set to zero. The MILP formulation given below, solved at this particular point of time, simultaneously determines the routes of both the vehicles to serve the remaining customers. It may be noted that while the first vehicle leaves customer location J and returns to the depot, the second vehicle leaves from and returns to the depot.

In order to utilize the MILP formulation given above, which requires all routes to begin from and end at the depot, a fictitious route is constructed from the depot to customer location J for the first vehicle with delivery and pickup loads of FG and RT, respectively. This ensures that the first vehicle indeed leaves from customer location J where it is currently situated. The objective function is suitably modified by subtracting the fictitious distance travelled by the first vehicle from the depot to customer location J.

In addition to the notations introduced earlier, the following notations have been added/modified.

Index

k set of vehicles:  $\{1, 2\}$ 

Data

J	current customer location of the first vehicle
FG	current delivery load of the first vehicle
RT	current pickup load of the first vehicle

#### Decision variable

 $x_{ijk}$  number of times vehicle k moves from customer i to customer j

The MILP formulation is given below.

Minimize	$C_{ij}X_{ijk}$ $C_{0J}$	$x_{0J1}$	
Subject to	$\begin{array}{ccc} y_{ij} & y_{ji} & d_j \\ i & i \end{array}$	j	(2.1)
	$egin{array}{ccc} z_{ji} & z_{ij} & r_{j} \ & & & i \end{array}$	j	(2.2)
	$y_{0J}$ FG		(2.3)
	$z_{0J}$ RT		(2.4)
	$y_{i0} = 0$		(2.5)
	$z_{0j}$ <b>R</b> T		(2.6)
	$\begin{array}{c} x_{ijk} & x_{jik} & 0 \\ x_{ijk} & i & 0 \end{array}$	j,k	(2.7)
	$x_{0jk} = 1$	k	(2.8)
	$x_{0J1} = 1$		(2.9)
	$y_{ij}$ $z_{ij}$ $v$ $x_{ijk}$	i, j	(2.10)
	$y_{ij}, z_{ij} = 0$	<i>i</i> , <i>j</i>	
	$x_{ijk}$ 0,1,2	i, j, k	

As already noted, the distance from the depot to customer location J is subtracted from the objective function to eliminate the effect of the fictitious route. This, of course, being a constant, would not have affected the routes of the two vehicles. Constraints (2.1), (2.2), (2.5), (2.7), (2.8) and (2.10) are analogous to Constraints (1.1), (1.2), (1.3), (1.5), (1.6) and (1.7), respectively, of the previous MILP formulation. Constraints (2.3) and (2.4) ensure that *FG* units of finished goods and *RT* units of returns are moved on the fictitious route from the depot to customer location *J* where the first vehicle is currently situated. Constraint (2.6) ensures that exactly *RT* units of returns leave the depot. Finally, Constraint (2.9) represents the fictitious route of the first vehicle from the depot to customer location *J*. We note here that Constraint (2.10) represents the aggregate capacity constraint on multiple visits of the vehicles, which for trivial problems, say with one depot and one customer, may not ensure that the vehicle capacity is not exceeded on individual visits. However, for more general problems with more number of customers with

Once the above formulation is solved, the distance travelled by the vehicles is added to the distance already travelled by the first vehicle to obtain the total distance travelled by both the vehicles.

#### 3.3 A greedy search algorithm for the static policy

Similar to the MILP formulation for the static policy, the algorithm (in line with the algorithm proposed in [13]) has to be run twice to determine the routes of the two vehicles. In addition to the previous notations, the following are also introduced.

no_of_customers	number of customers to be served by the vehicle
DL	delivery load of the vehicle
PL	pickup load of the vehicle
cumul_PL	cumulative pickup load of the vehicle
total_dist	total distance travelled by the vehicle

*cumul\_PL* is the total pickup load on the route of the vehicle. When the vehicle leaves the depot, its *DL* is equal to the cumulative delivery load on its route and its *PL* is zero. On the other hand, when the vehicle returns to the depot, its *DL* is zero and its *PL* is equal to *cumul\_PL*. *DL* and *PL* get updated every time the vehicle visits a customer depending on its delivery and pickup demands.

The pseudo-code of the algorithm is given below, followed by explanations.

1. i = 0 (set the initial location of the vehicle as the depot)

3. For j = 1 to j no\_of\_customers Step 1

- 4. If  $d_j > 0$  or  $(r_j > 0$  and DL + PL < v) then
- 5. If  $c_{ij} < min_{dist}$  (minimum distance obtained so far from i to a customer)
- 6. then  $next\_dest = j$  and  $min\_dist = c_{ij}$

(set j as the next destination and  $c_{ij}$  as the new minimum distance)

7. Otherwise if  $c_{ij} = min\_dist$  then

11.

4.2 Generation of customers' delivery and pickup demands

## Instance 1

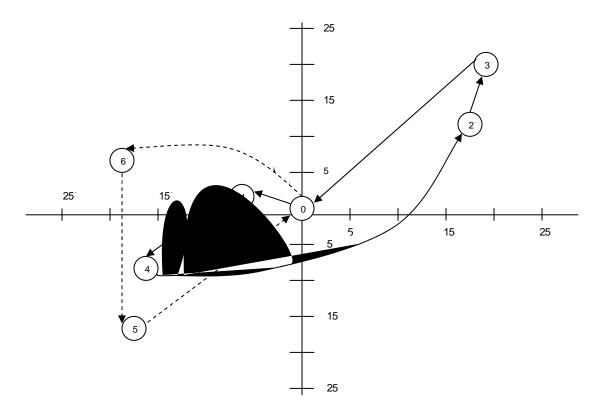
.

To demonstrate, suppose the delivery and pickup demands of Customers 1-4 are available in the beginning, and the same information on Customers 5 and 6 are availa

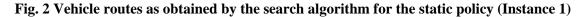
Vehicle	Route	Delivery load	Pickup load	
	0 - 4	0.64	0	
	4 - 1	0.28	0.13	
1	1 – 3	0.23	0.35	
	3 - 2	0.16	0.56	
	2 - 0	0	0.66	
	0-5	0.36	0	
2	5 - 6	0.31	0.30	
	6 - 0	0	0.34	

Table 3 Delivery and pickup loads of the vehicles as obtained by the MILP formulation for<br/>the static policy (Instance 1)

The total distance travelled by the two vehicles is 155.39 km obtained by the MILP formulation for the static policy. Next, the proposed search algorithm is applied to the data, which gives the routes of the vehicles and their delivery and pickup loads, as shown by Fig. 2 and Table 4, respectively.



Route of the first vehicle Route of the second vehicle



Vehicle	Route	Delivery load	Pickup load
	0 - 1	0.64	0
	1 - 4	0.59	0.22
1	4 - 2	0.23	0.35
	2 - 3	0.07	0.45
	3 - 0	0	0.66
	0-6	0.36	0
2	6 - 5	0.05	0.04
	5 - 0	0	0.34

Table 4 Delivery and pickup loads of the vehicles as obtained by the search algorithm for<br/>the static policy (Instance 1)

The total distance travelled by the two vehicles is 157.75 km obtained by the search algorithm for the static policy, which compares well with the total distance travelled by the two vehicles obtained by the MILP formulation for the static policy.

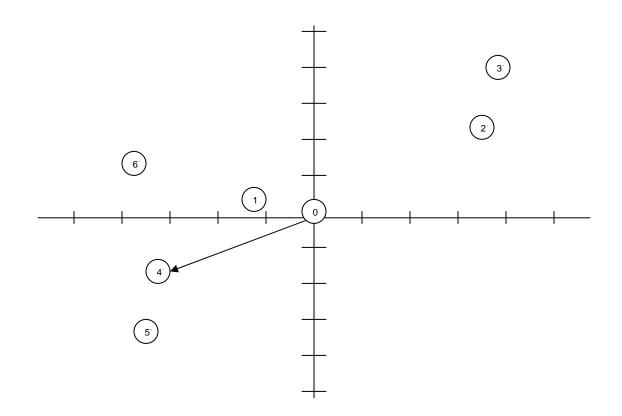
To apply the dynamic policy, suppose the first vehicle has already served Customers 4 and 1, and is currently located at Customer 3 with delivery and pickup loads of 0.23 and 0.35, respectively, (Fig. 1 and Table 3) when demand information fr

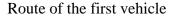
Route of the first vehicle

Route of the second vehicle

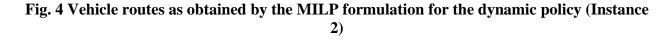
Fig. 3 Vehicle routes as obtained by the MILP

Now, for the dynamic policy, suppose the first vehicle has already served Customers 4 and 5, and is currently located at Customer 6 with delivery and pickup loads of 0.38 and 0.43, respectively, when demand information from Customers 1 and 2 become available. By applying the MILP formulation for the dynamic policy, we obtain the vehicle routes and the delivery and pickup loads carried by the vehicles, as shown by Fig. 4 and Table 6, respectively.





Route of the second vehicle



Vehicle	Route	Delivery load	Pickup load
	0 - 4	0.79	0
1	4 - 5	0.43	0.13
1	5 - 6	0.38	0.43
	6 – 1	0.07	0.47
	1 - 0	0	0.69
	0 - 1	0.21	0
2	1 – 3	0.23	0
	3 - 2	0.16	0.21
	2 - 0	0	0.31

Table 6 Delivery and pickup loads of the vehicles as obtained by the MILP formulation for<br/>the dynamic policy (Instance 2)

Note that in this case there is an overlap at Customer 1, i.e. both vehicles serve Customer 1. The total distance travelled by the vehicles is 132.75 km obtained by the MILP formulation for the dynamic policy, which is lower than that obtained by the formulation for the static policy.

When the search algorithm for the dynamic policy is applied to the same data, we get the vehicle routes and the delivery and pickup loads of the vehicles, as shown by Fig. 5 and Table 7, respectively.

policy. Although, the total distance travelled for the dynamic policy is slightly lower than that for the static policy, the saving is not comparable with the saving obtained by the MILP formulation. This is due to the structural differences between the MILP formulation and the search algorithm. The MILP formulation is less constrained than the search algorithm. It may be noted from Table 6 that the first vehicle actually leaves 0.02 units of delivery load at Customer 1, which is later picked up by the second vehicle. However, to make such a provision in the search algorithm, a more complicated logic has to be built, which in its present form has been kept as simple as possible with the shortest distance being the primary criterion for the selection of the next customer on the route.

#### 4.3.1 Experimentation with 6 customers

Since the problem is known to be NP-Hard, the MILP formulation fails to produce optimal solutions to problems with a larger number of customers in a reasonable amount of time. Also, because the search algorithm performs reasonably well vis-à-vis the MILP formulation for small-to-medium-sized problems [13], henceforth we use this algorithm for solving vehicle routing problems with backhauling and dynamically arising customer demands.

We experimented with different combinations of customer locations and their delivery and pickup demands. Since the results are similar, we present here the results of one experimental set-up with customer locations given in Table 1.

Given the experimental set-up of the amount of demand information available in the beginning (from 4 customers) and later (from the remaining 2 customers), we can create a total of 15

Customer	Delivery demand	Pickup demand	
1	0.06	0.20	
2	0.30	0.11	
3	0.08	0.21	
4	0.16	0.14	
5	0.36	0.21	
6	0.04	0.13	

Table 8 Delivery and pickup demands of customers as fractions of vehicle capacity (Set 2)

# Table 9 Total distances (km) travelled by the vehicles for 2 data sets for the static and dynamic policies

	Demand	Demand	Total distance (km) travelled by the vehicles					
Problem	information	ormation information		Data Set 1 (Table 2)			Data Set 2 (Table 8)	
instance	available nstance first from	available later from customers	Static	Dynamic	Dynamic/ Static	Static	Dynamic	Dynamic/ Static
1	1, 2, 3, 4	5, 6	157.75	157.75	1	190.74	190.74	1
2	2, 3, 4, 5	1,6	145.43	145.43	1	181.97	187.35	1.03
3	1, 3, 4, 5	2, 6	183.52	161.65	0.88	168.02	168.02	1
4	1, 2, 4, 5	3, 6	180.42	161.65	0.90	180.82	187.35	1.04
5	1, 2, 3, 5	4, 6	157.13	157.13	1	190.24	190.24	1
6	2, 3, 4, 6	1, 5	153.30	153.30	1	221.29	181.85	0.82
7	1, 3, 4, 6	2, 5	189.06	177.02	0.94	178.98	172.85	0.97
8	1, 2, 4, 6	3, 5	206.20	191.06	0.93	203.78	210.73	1.03
9	1, 2, 3, 6	4, 5	141.60	141.60	1	157.27	172.85	1.10
10	3, 4, 5, 6	1, 2	166.94	165.31	0.99	193.60	193.60	1
11	2, 4, 5, 6	1, 3	168.93	165.31	0.98	161.20	161.20	1
12	2, 3, 5, 6	1,4	157.68	157.68	1	227.56	219.95	0.97
13	1, 4, 5, 6	2, 3	126.01	126.01	1	196.83	196.83	1
14	1, 3, 5, 6	2,4	196.19	158.47	0.81	172.44	172.44	1
15	1, 2, 5, 6	3, 4	195.42	158.47	0.81	210.32	210.32	1

The column 'Dynamic/Static' gives the ratios of the total distances travelled by the dynamic policy by those by the static policy. It may be observed from Table 9 that for Set 1 the dynamic policy performs at least as good as the static policy whereas for Set 2 there are 4 instances where the dynamic policy is outperformed by the static policy. This may be treated as an aberration as

dynamic policies are indeed at least as good as static policies, and can be attributed to the limitation of the search algorithm of not being able to ensure the same. In case such an aberration happens, we simply revert to the static policy.

We observe from Table 9 that the dynamic policy outperforms the static policy in only 11 of the 30 problem instances (36.67%), and also out of these 11 instances, there are only a few where the savings could be considered substantial. A t-test also confirmed that the null hypothesis that there is no difference between the static and dynamic policies could not be rejected at 1% level of significance.

#### 4.3.2 Experimentation with 20 customers

The experimentation with 6 customers can only indicate the relative performances of the static and dynamic policies. However, the quantum of demand information available in the beginning and how early or late the demand information from the remaining customers becomes available when the first vehicle is still in service might also have impacted the performances of the static and dynamic policies, which could not be tested with only 6 customers in the problem sets. Therefore, we consider a problem with 20 customers for which the locations and the delivery and pickup demands are generated in the same way as before, and are represented by Table A.1 and Table A.2, respectively, in Appendix A. We restrict to 20 customers because of two reasons. First, we consider only small-to-medium-sized problems, and second, as already mentioned, the performance of the search algorithm compared well with that of the MILP formulation for problem sizes of up to 20 customers [13] beyond which the MILP formulation failed to deliver solutions in a reasonable amount of time. Since the performance of the algorithm could not be compared with that of the MILP formulation beyond 20 customers, we limit the problem size to 20 customers in this paper. However, it is possible to extend the search algorithm for solving larger problems.

We, of course, experimented with different combinations of customer locations, their delivery and pickup demands, and dynamic information availability, and obtained similar results. We present the results of one experimental set-up here. We consider 2 scenarios - a) Demand information from Customers 1-15 are available in the

#### 4.4 Discussions

From the numerical experimentations, we derive the following observations:

- a) For a small number of customers, it may not be worthwhile to deploy the dynamic policy because its cost advantage over the static policy may not be able to outweigh the additional effort to be put in for its deployment.
- b) Both static and dynamic policies perform better when less demand information is available at the beginning of the period and more is revealed at a later point of time during the period.
- c) The advantage of the dynamic policy over the static policy is more significant when new customer requests arise at an earlier point of time during the period.
- d) Given the same point of time of the arrival of new customer requests, the advantage of the dynamic policy over the static policy is more pronounced for the situation when less demand information is available at the beginning of the period. This corroborates the observation in *Lund et al.* [12] that static policies still perform relatively well for low degrees of dynamism (*dod*).

The above-mentioned observations are based on specific problem sizes (small-to-medium) and instances, and hence cannot be generalized. They are at best conjectures, the validity of which needs to be established by means of extensive numerical experimentations with larger problem sizes. Nevertheless, we hope that the results obtained in this paper through limited numerical experimentations would provide a platform to explore the trade-off between static and dynamic policies in further detail.

#### 5 Conclusions and directions for future research

Although the dynamic VRP has attracted the attention of many researchers, there has been limited attention to the dynamic VRPB in the literature so far. The objective of this paper has been to compare between static and dynamic policies for the dynamic VRPB. We have developed the MILP formulations and a search algorithm for the dynamic VRPB under consideration. Experimentations with a small-to-medium number of customer locations have shown that the static policy may perform reasonably well for a small number of customers and low degrees of dynamism (*dod* 

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Appendix A

Customer	Delivery demand	Pickup demand
1	0.11	0.07
2	0.06	0.04
3	0.01	0.01
4	0.10	0.10
5	0.04	0.10
6	0.00	0.01
7	0.11	0.01
8	0.00	0.09
9	0.09	0.00
10	0.00	0.08
11	0.02	0.01
12	0.06	0.09
13	0.06	0.05
14	0.12	0.02
15	0.05	0.06
16	0.08	0.06
17	0.03	0.04
18	0.03	0.05
19	0.03	0.01
20	0.00	0.08

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Table A.2 Delivery and pickup demands of customers as fractions of vehicle capacity (20 Customers)